

## Task 1

Convert the following numbers to decimal:

Binary:

1. 00110101
2. 00001010
3. 00101111
4. 10001000

Hexadecimal:

1. 41
2. 61
3. 7A
4. FF

## Task 1 Solution

The way to convert from binary to decimal is the same as convert from base-2 to base-10:

$$00110101_2 = [(0) \cdot 2^7] + [(0) \cdot 2^6] + [(1) \cdot 2^5] + [(1) \cdot 2^4] + [(0) \cdot 2^3] + [(1) \cdot 2^2] + [(0) \cdot 2^1] + [(1) \cdot 2^0] = 53$$

Binary:

1. 53
2. 10
3. 47
4. 136

The way to convert from hexadecimal to decimal is the same as convert from base-16 to base-10:

$$41_{16} = [(4) \cdot 16^1] + [(1) \cdot 16^0] = 65$$

Hexadecimal:

1. 65
2. 97
3. 122
4. 255

## Task 2

What is the symbol of the following ASCII codes:

Hexadecimal:

1. 0A
2. 0D
3. 41
4. 61

Decimal:

1. 48
2. 49
3. 92

## Task 2 Solution

Hexadecimal:

1. LF (Line feed, new line)
2. CR (Carriage return)
3. A
4. a

Decimal:

1. 0
2. 1
3. \

## Task 3

Consider a byte which stores a signed number in the range -128 to 127. Negative numbers are represented as two's complement.

The binary representation of the number 3 is 00000011, while the number -3 is the two's complement 11111101.

What is the binary representation of the following numbers:

0, 1, 10, 16, 32, 64, -1, -2, -10, -16, -32, -64

## Task 3 Solution

$$\begin{aligned} 0 &= 00000000_2 \\ 1 &= 00000001_2 \\ 10 &= 00001010_2 \\ 16 &= 00010000_2 \\ 32 &= 00100000_2 \\ 64 &= 01000000_2 \end{aligned}$$

Since this is represented in a byte there are 8 bits.

Using two's complement to find the negative of the number. Invert the bits and add 1. For instance -1:

$$\begin{array}{r|l} 00000001 & = 1 \\ \neg 11111110 & = -2 \\ +1 11111111 & = -1 \end{array}$$

Table 1: Two's complement of 1

$$\begin{aligned} -1 &= 11111111_2 \\ -10 &= 11110110_2 \\ -16 &= 11110000_2 \\ -32 &= 11100000_2 \\ -64 &= 11000000_2 \end{aligned}$$

## Task 4

### Task 4.a

Show with a truth table that

$$\begin{aligned} A + B + (A \cdot \bar{B}) &= A + B \\ (A + B) \cdot (A + \bar{B}) &= A \end{aligned}$$

### Task 4.b

Draw logical gates for both sides of de Morgan's laws

$$\begin{aligned} \overline{A + B} &= \bar{A} \cdot \bar{B} \\ \overline{A \cdot B} &= \bar{A} + \bar{B} \end{aligned}$$

## Task 4 Solution

### Task 4.a Solution

We can see that column 3 and 5 are equal in Table 2.

A	B	$A + B$	$A \cdot \overline{B}$	$A + B + (A \cdot \overline{B})$
0	0	0	0	0
0	1	1	0	1
1	0	1	1	1
1	1	1	0	1

Table 2: Truth table for  $A + B + (A \cdot \overline{B}) = A + B$

We can see that column 1 and 5 are equal in Table 3.

A	B	$A + B$	$A + \overline{B}$	$(A + B) \cdot (A + \overline{B})$
0	0	0	1	0
0	1	1	0	0
1	0	1	1	1
1	1	1	1	1

Table 3: Truth table for  $(A + B) \cdot (A + \overline{B}) = A$

### Task 4.b Solution

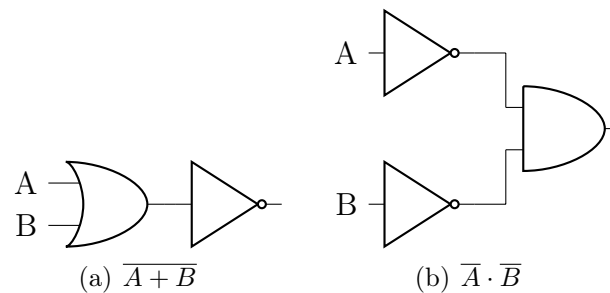


Figure 1: Logic gates for  $\overline{A + B} = \overline{A} \cdot \overline{B}$

## Task 5

Suppose that the three-phase voltages are in Figure 3 are:

$$\begin{aligned}
 v_a(t) &= \sqrt{2}V_P \cos(\omega t) \\
 v_b(t) &= \sqrt{2}V_P \cos\left(\omega t - \frac{2\pi}{3}\right) \\
 v_c(t) &= \sqrt{2}V_P \cos\left(\omega t - \frac{4\pi}{3}\right)
 \end{aligned}$$

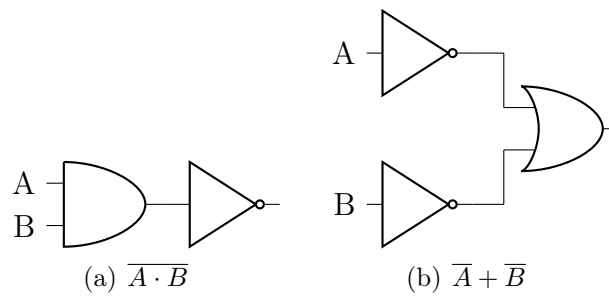


Figure 2: Logic gates for  $\overline{A \cdot B} = \overline{A} + \overline{B}$

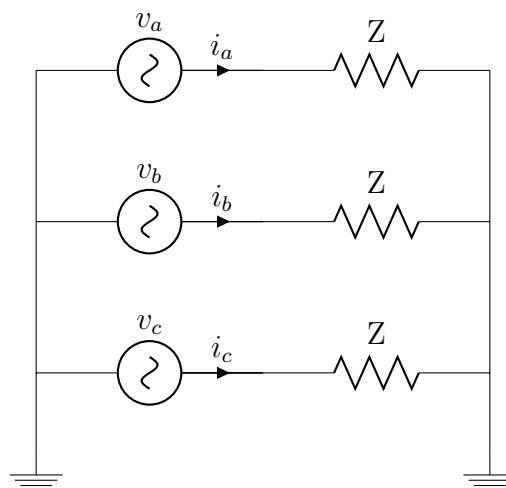


Figure 3: Three phase circuit

While the phasor representations are:

$$\begin{aligned} \mathbb{V}_a(t) &= V_P e^{j0} \\ \mathbb{V}_b(t) &= V_P e^{-j\frac{2\pi}{3}} \\ \mathbb{V}_c(t) &= V_P e^{-j\frac{4\pi}{3}} \end{aligned}$$

### Task 5.a

Suppose that the impedance is real and given by  $Z = 230 \Omega$  and  $V_P = 230 \text{ V}$ . Find the current  $i_a$ ,  $i_b$  and  $i_c$  and the corresponding phasors  $\mathbb{I}_a$ ,  $\mathbb{I}_b$  and  $\mathbb{I}_c$ .

### Task 5.b

What is the power delivered to the impedances?

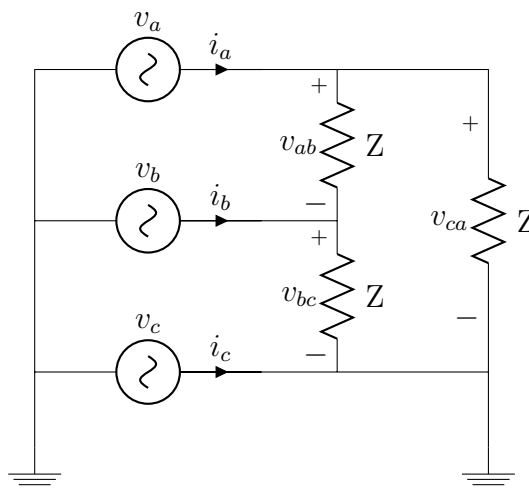


Figure 4: Three phase circuit

### Task 5.c

Find  $v_{ab}$ ,  $v_{bc}$  and  $v_{ca}$  and the corresponding phasors  $\mathbb{V}_{ab}$ ,  $\mathbb{V}_{bc}$  and  $\mathbb{V}_{ca}$  in Figure 4.

### Task 5.d

Find the currents  $i_{ab}$ ,  $i_{bc}$  and  $i_{ca}$  and the corresponding phasors  $\mathbb{I}_{ab}$ ,  $\mathbb{I}_{bc}$  and  $\mathbb{I}_{ca}$  with  $Z$  and  $V_P$  as given in Task 5.a.

### Task 5.e

What is the power delivered to the impedances?

## Task 5 Solution

### Task 5.a Solution

Since  $\mathbb{Z}$  is real we can use  $v_a = \mathbb{Z}i_a$  with the same for b and c. This means that:

$$\begin{aligned}i_a(t) &= \sqrt{2} \frac{V_P}{\mathbb{Z}} \cos(\omega t) = \sqrt{2} \frac{230}{230} \cos(\omega t) = \underline{\underline{\sqrt{2} \cos(\omega t)}} \\i_b(t) &= \sqrt{2} \frac{V_P}{\mathbb{Z}} \cos\left(\omega t - \frac{2\pi}{3}\right) = \sqrt{2} \frac{230}{230} \cos\left(\omega t - \frac{2\pi}{3}\right) = \underline{\underline{\sqrt{2} \cos\left(\omega t - \frac{2\pi}{3}\right)}} \\i_c(t) &= \sqrt{2} \frac{V_P}{\mathbb{Z}} \cos\left(\omega t - \frac{4\pi}{3}\right) = \sqrt{2} \frac{230}{230} \cos\left(\omega t - \frac{4\pi}{3}\right) = \underline{\underline{\sqrt{2} \cos\left(\omega t - \frac{4\pi}{3}\right)}}\end{aligned}$$

While the phasor representations are:

$$\begin{aligned}\mathbb{I}_a(t) &= \frac{V_P}{\mathbb{Z}} e^{j0} = \frac{230}{230} e^{j0} = \underline{\underline{e^{j0}}} \\ \mathbb{I}_b(t) &= \frac{V_P}{\mathbb{Z}} e^{-j\frac{2\pi}{3}} = \frac{230}{230} e^{-j\frac{2\pi}{3}} = \underline{\underline{e^{-j\frac{2\pi}{3}}}} \\ \mathbb{I}_c(t) &= \frac{V_P}{\mathbb{Z}} e^{-j\frac{4\pi}{3}} = \frac{230}{230} e^{-j\frac{4\pi}{3}} = \underline{\underline{-e^{j\frac{4\pi}{3}}}}\end{aligned}$$

### Task 5.b Solution

$$\begin{aligned}P_a &= V_a I_a = \sqrt{2} V_P \cos(\omega t) \sqrt{2} \cos(\omega t) = \underline{\underline{2V_P \cos^2(\omega t)}} \\ P_b &= V_b I_b = \sqrt{2} V_P \cos\left(\omega t - \frac{2\pi}{3}\right) \sqrt{2} \cos\left(\omega t - \frac{2\pi}{3}\right) = \underline{\underline{2V_P \cos^2\left(\omega t - \frac{2\pi}{3}\right)}} \\ P_c &= V_c I_c = \sqrt{2} V_P \cos\left(\omega t - \frac{4\pi}{3}\right) \sqrt{2} \cos\left(\omega t - \frac{4\pi}{3}\right) = \underline{\underline{2V_P \cos^2\left(\omega t - \frac{4\pi}{3}\right)}}\end{aligned}$$

**Task 5.c Solution**

$$\begin{aligned}
 v_{ab} &= v_a - v_b = \sqrt{2}V_P \cos(\omega t) - \sqrt{2}V_P \cos(\omega t - \frac{2\pi}{3}) = \sqrt{2}V_P \cdot -2\sin(\omega t - \frac{\pi}{3})\sin(\frac{\pi}{3}) \\
 &= \underline{\underline{-\sqrt{6}V_P \sin(\omega t - \frac{\pi}{3})}} \\
 v_{bc} &= v_b - v_c = \sqrt{2}V_P \cos(\omega t - \frac{2\pi}{3}) - \sqrt{2}V_P \cos(\omega t - \frac{4\pi}{3}) = \sqrt{2}V_P \cdot -2\sin(\omega t - \pi)\sin(\frac{-\pi}{3}) \\
 &= \underline{\underline{-\sqrt{6}V_P \sin(\omega t - \pi)}} \\
 v_{ca} &= v_c - v_a = \sqrt{2}V_P \cos(\omega t - \frac{4\pi}{3}) - \sqrt{2}V_P \cos(\omega t) = \sqrt{2}V_P \cdot -2\sin(\omega t - \frac{2\pi}{3})\sin(\frac{-2\pi}{3}) \\
 &= \underline{\underline{\sqrt{6}V_P \sin(\omega t - \frac{2\pi}{3})}}
 \end{aligned}$$

$$\begin{aligned}
 \mathbb{V}_{ab} &= \mathbb{V}_a - \mathbb{V}_b = V_P(e^{j0} - e^{-j\frac{2\pi}{3}}) = \underline{\underline{\sqrt{3}V_P e^{j\frac{\pi}{6}}}} \\
 \mathbb{V}_{bc} &= \mathbb{V}_b - \mathbb{V}_c = V_P(e^{-j\frac{2\pi}{3}} - e^{-j\frac{4\pi}{3}}) = \underline{\underline{\sqrt{3}V_P e^{-j\frac{\pi}{2}}}} \\
 \mathbb{V}_{ca} &= \mathbb{V}_c - \mathbb{V}_a = V_P(e^{-j\frac{4\pi}{3}} - e^{j0}) = \underline{\underline{\sqrt{3}V_P e^{j\frac{-7\pi}{6}}}}
 \end{aligned}$$

**Task 5.d Solution**

$$\begin{aligned}
 i_{ab} &= \frac{v_{ab}}{\mathbb{Z}} = -\sqrt{6}\frac{230}{230}\sin(\omega t - \frac{\pi}{3}) = \underline{\underline{-\sqrt{6}\sin(\omega t - \frac{\pi}{3})}} \\
 i_{bc} &= \frac{v_{bc}}{\mathbb{Z}} = -\sqrt{6}\frac{230}{230}\sin(\omega t - \pi) = \underline{\underline{-\sqrt{6}\sin(\omega t - \pi)}} \\
 i_{ca} &= \frac{v_{ca}}{\mathbb{Z}} = \sqrt{6}\frac{230}{230}\sin(\omega t - \frac{2\pi}{3}) = \underline{\underline{\sqrt{6}\sin(\omega t - \frac{2\pi}{3})}}
 \end{aligned}$$

$$\begin{aligned}
 \mathbb{I}_{ab} &= \sqrt{3}\frac{230}{230}e^{j\frac{-\pi}{6}} = \underline{\underline{\sqrt{3}e^{j\frac{\pi}{6}}}} \\
 \mathbb{I}_{bc} &= \sqrt{3}\frac{230}{230}e^{j\frac{-\pi}{2}} = \underline{\underline{\sqrt{3}e^{-j\frac{\pi}{2}}}} \\
 \mathbb{I}_{ca} &= \sqrt{3}\frac{230}{230}e^{j\frac{-7\pi}{6}} = \underline{\underline{\sqrt{3}e^{j\frac{-7\pi}{6}}}}
 \end{aligned}$$



**Task 5.e Solution**

$$P_{ab} = v_{ab}i_{ab} = -230\sqrt{6}\sin(\omega t - \frac{\pi}{3})\sqrt{6}\sin(\omega t - \frac{\pi}{3}) = \underline{\underline{-1380\sin^2(\omega t - \frac{\pi}{3})}}$$

$$P_{bc} = v_{bc}i_{bc} = -230\sqrt{6}\sin(\omega t - \pi)\sqrt{6}\sin(\omega t - \pi) = \underline{\underline{-1380\sin^2(\omega t - \pi)}}$$

$$P_{ca} = v_{ca}i_{ca} = 230\sqrt{6}\sin(\omega t - \frac{2\pi}{3})\sqrt{6}\sin(\omega t - \frac{2\pi}{3}) = \underline{\underline{1380\sin^2(\omega t - \frac{2\pi}{3})}}$$